

## Lost in space

**Question:** A collection of  $N$  asteroids floats in space far from other gravitating bodies. Model each asteroid as a hard sphere of radius  $R$  and mass  $m$ . What quantities are required for a macroscopic description of this system?

A **microscopic** description consists of two pieces:

- The mechanical parameters  $N$ ,  $m$ ,  $R$ , plus Newton's law of gravity — these are the things we would need to know in order to write down the Hamiltonian.
- The dynamical variables  $\mathbf{r}_1, \mathbf{r}_2, \dots, \mathbf{r}_N$  and  $\mathbf{p}_1, \mathbf{p}_2, \dots, \mathbf{p}_N$  — these are the things we would solve for if this were a classical mechanics problem.

A **macroscopic** description also consists of two pieces:

- The same mechanical parameters as before.
- The conserved quantities  $E$  (energy),  $\mathbf{P}$  (total momentum), and  $\mathbf{L}$  (total angular momentum). (For a box of gas molecules the external wall forces mean that  $\mathbf{P}$  and  $\mathbf{L}$  are not conserved, so they don't become part of the macroscopic description. But for the asteroid case they *are* conserved and hence *are* part of the macroscopic description.)

In the microscopic description  $6N$  dynamical variables are specified, whereas in the macroscopic description 7 conserved quantities are specified.